



(Knowledge for Development)

**KIBABII UNIVERSITY**  
**UNIVERSITY EXAMINATIONS**  
**2017/2018 ACADEMIC YEAR**  
**FIRST YEAR SECOND SEMESTER**  
**SPECIAL/ SUPPLEMENTARY EXAMINATION**  
**FOR THE DEGREE OF MASTER OF SCIENCE IN**  
**STATISTICS**

**COURSE CODE:** STA 851

**COURSE TITLE:** CATEGORICAL DATA ANALYSIS

**DATE:** 12/08/10/18

**TIME:** 8 AM -11 AM

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**INSTRUCTIONS TO CANDIDATES**

Answer Question One and Any Other TWO Questions

TIME: 3 Hours

This Paper Consists of 4 Printed Pages. Please Turn Over.

**QUESTION ONE (30 MARKS)**

(a) Explain the following terms us used in categorical data analysis

- (i) Response variable
- (ii) Nominal variable
- (iii) Relative risk
- (iv) Odds ratio

(b) Explain in details the main probability distribution models in categorical data analysis

The following table was taken from the General Social Survey:

Belief in Afterlife

Race	Yes	No or Undecided	Total
White	31	12	43
Black	9	4	13

Find the relative risk and the 95% approximate confidence interval for the true value of the relative risk.  
( $z_{.95} = 1.645$ ;  $z_{.975} = 1.96$ )

**QUESTION TWO (20 Marks)**

In the United States, the estimated annual probability that a woman over the age of 35 dies of lung cancer equals 0.001304 for current smokers and 0.000121 for nonsmokers *JM. Pagano and K. Gauvreau, Principles of Biostatistics*, Duxbury Press, Pacific Grove, CA. 1993, p. 134..

- a. Find and interpret the difference of proportions and the relative risk. Which measure is more informative for these data? Why?
- b. Find and interpret the odds ratio. Explain why the relative risk and odds ratio take similar values.

**QUESTION THREE (20 MKS )**

The Table below shows the results of a retrospective study comparing radiation therapy with surgery in treating cancer of the larynx. The response

**TABLE 3.13 Data for Problem 3.13**

	Cancer Controlled	Cancer Not Controlled
Surgery	21	2
Radiation therapy	15	3

Source: Reprinted with permission from W. M. Mendenhall, R. R. Million, D. E. Sharkey, and N. J. Cassisi, *Internat. J.*

SAS OUTPUT

Fisher's Exact Test		
Cell (1,1) Frequency (F)		21
Left-sided Pr <= F		0.8947
Right-sided Pr >= F		0.3808
Table Probability (P)		0.2755
Two-sided Pr<= P		0.6384
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Odds Ratio		2.1000
Asymptotic Conf Limits:	95% Lower Conf Limit	0.3116
	95% Upper Conf Limit	14.1523
Exact Conf Limits:	95% Lower Conf Limit	0.2089
	95% Upper Conf Limit	27.5522

indicates whether the cancer was controlled for at least two years following treatment.

- Report and interpret the  $P$ -value for Fisher's exact test with  $H_0: \theta = 1$ , and  $H_a: \theta > 1$ . Explain how the  $P$ -values are calculated.
- Interpret the confidence intervals for  $\theta$ . Explain the difference between them and how they were calculated.
- Find and interpret the one-sided mid- $P$ -value. Give advantages and disadvantages of this type of  $P$ -value.

**QUESTION FOUR (20 MKS )**

- Describe the purpose of the link function of a GLM. What is the identity link? Explain why it is not often used with binomial or Poisson responses.
- Explain how logistic regression model is applied in categorical data analysis

QUESTION FIVE (20 MKS )

Suppose we have the following three-way contingency table:

Victim's Race	Defendant's Race	Death Penalty		Total
		Yes	No	
White	White	2	13	15
	Black	1	5	6
	Total	3	18	21
Black	White	0	5	5
	Black	1	15	16
	Total	1	20	21

- (a). Compute and interpret the sample conditional odds ratios, adding 0.5 to each cell to reduce the impact of the 0 cell count.
- (b). Test the hypothesis that death penalty is independent of defendant's race, controlling for victim's race using the Cochran-Mantel-Haenszel test with  $\alpha = 5\%$ . ( $\chi^2(.95) = 3.8415, \chi^2(.95)$ )