

We show that a Banach space with separable dual can be renormed to satisfy hereditarily an "almost" optimal uniform smoothness condition. The optimal condition occurs when the canonical decomposition $X^{**} = X \oplus X^{\perp}$ is unconditional. Motivated by this result, we define a subspace X of a Banach space Y to be an h -ideal (resp. a u -ideal) if there is an hermitian projection P (resp. a projection P with $\|I - 2P\| = 1$) on Y^* with kernel X^{\perp} . We undertake a general study of h -ideals and u -ideals. For example we show that if a separable Banach space X is an h -ideal in X^{**} then X has the complex form of Pełczyński's property (u) with constant one and the Baire-one functions $Ba(X)$ in X^{**} are complemented by an hermitian projection; the converse holds under a compatibility condition which is shown to be necessary. We relate these ideas to the more familiar notion of an M -ideal, and to Banach lattices. We further investigate when, for a separable Banach space X , the ideal of compact operators $K(X)$ is a u -ideal or an h -ideal in $\mathcal{L}(X)$ or $K(X)^{**}$. For example, we show that $K(X)$ is an h -ideal in $K(X)^{**}$ if and only if X has the "unconditional compact approximation property" and X is an M -ideal in X^{**} .