



KIBABII UNIVERSITY

UNIVERSITY EXAMINATIONS
2020/2022 ACADEMIC YEAR

SECOND YEAR FIRST SEMESTER
SUPPLEMENTARY/SPECIAL EXAMINATIONS

FOR THE DEGREE OF B.Ed. (SCIENCE)

COURSE CODE: SPH 221

COURSE TITLE: ELECTRICITY AND MAGNETISM II

DURATION: 2 HOURS

DATE: 29/07/2022

TIME: 2:00PM-4:00PM

INSTRUCTIONS TO CANDIDATES

- Answer **QUESTION ONE** (Compulsory) and any other two (2) Questions.
- The following constants might be used: $K_e=8.99 \times 10^9 \text{ N.m}^2/\text{C}^2$; $M_e=9.1 \times 10^{-31} \text{ kg}$; $M_p=1.6 \times 10^{-27} \text{ kg}$; $e=1.60 \times 10^{-19} \text{ C}$; $\epsilon_0=8.85 \times 10^{-12} \text{ C}^2/\text{N.M}^2$

KIBU observes ZERO tolerance to examination cheating

SPH 221: Electricity and Magnetism II

QUESTION ONE [30 Marks]

- a) Give an expression relating the magnitude of electric force between two charged particles. [2]
- b) The electron and proton of hydrogen atom are separated by a distance of approximately 5.3×10^{-11} m. Find the magnitude of electric force exerted on the particles. [3]
- c) A dust particle with mass $m_1 = 4 \mu\text{g}$ and charge $q_1 = 7 \mu\text{C}$ is 3 cm away from another particle with mass $m_2 = 8 \mu\text{g}$ and $q_2 = 5 \mu\text{C}$. Find the acceleration for each. [4]
- d) Define electric field at a point in space. [2]
- e) What is capacitance of a capacitor? [2]
- f) Show that for two capacitors in parallel, the equivalent capacitance is given by $C = C_1 + C_2$. [3]
- g) Show that for an insulating sphere of radius a with uniform charge density ρ and carries a positive charge Q , the electric field in region $r < a$ is given by $E = \frac{\rho}{3\epsilon_0} r$ [4]
- h) A parallel plate capacitor has an area of $A = 2.0 \times 10^{-4} \text{ m}^2$ and plate separation = 1.0 mm. Find its capacitance. [3]
- i) Show that the work done in charging a capacitor to a charge Q equals the electrical potential energy U stored in the capacitor i.e. $U = \frac{Q^2}{2C} = \frac{1}{2} Q \Delta V = \frac{1}{2} C (\Delta V)^2$ [4]
- j) A $5.0 \mu\text{F}$ capacitor is charged to a potential of 800V and then discharged through a $25 \text{K}\Omega$ resistor. How much energy is delivered to the resistor in time it takes to fully discharge the capacitor? [3]

QUESTION TWO [20 Marks]

- a) Utilizing the electric field due to a point charge, show that the electric flux Φ is given by $\Phi = \frac{q}{\epsilon_0}$ [3]
- b) A spherical shell with $R = 5 \text{ m}$ has a net charge of $Q = 1 \mu\text{C}$ uniformly distributed over the surface. What is the magnitude of the electric field at (a) a distance $r = 1 \text{ m}$ from the *center* of the sphere and (b) a distance $d = 1 \text{ m}$ from the *surface* of the sphere? [4]
- c) Show that the capacitance of a parallel plate capacitor is given by $C = \frac{\epsilon_0 A}{d}$ where ϵ_0 = permittivity of free space; A = area of the plates and d = plate separation. [4]
- d) Joule's heating in a resistor R is given as $P = i^2 R = \frac{\epsilon^2 R}{(R+r)^2}$ where ϵ = e.m.f of the cell and r is the internal resistance. What is the value of R to obtain maximum Joule's heating? [3]
- e) What is the force on $0.1 \mu\text{C}$ charge moving at velocity $\mathbf{v} = (10\mathbf{j} - 20\mathbf{k}) \text{ m/s}$ in a magnetic field $\mathbf{B} = (-3\mathbf{i} + 4\mathbf{k}) \times 10^{-4} \text{ T}$? [3]
- f) Consider a capacitor of capacitance C that is being discharged through a resistor of resistance R . After how many time constants is the charge on the capacitor one-fourth its initial value? [3]

QUESTION THREE [20 Marks]

- a) State the Kirchhoff's laws, as applied in complex circuit analysis [2]

- b) Find the currents I_1 , I_2 and I_3 in the circuit shown in figure 2. [8]

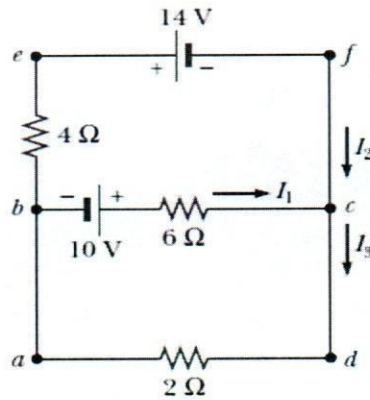


Figure 2

- c) Show that if a capacitor is charged with a battery through a resistor of resistance R , the current on the capacitor vary in time according to the expression $I(t) = \frac{\mathcal{E}}{R} e^{-\frac{t}{RC}}$. [10]

QUESTION FOUR [20 Marks]

- a) A proton is moving in a circular orbit of radius 14 cm in a uniform 0.35T magnetic field perpendicular to the velocity of the proton. Find the linear speed of the proton. [3]
- b) Give a mathematical expression of the Biot-Savart law? [2]
- c) Explain the origin of magnetic field that can be determined by the Biot-Savart law. [1]
- d) For a straight, long thin wire carrying a constant current i , determine the magnitude of magnetic field at a point P due to this current. [use figure 3] [8]

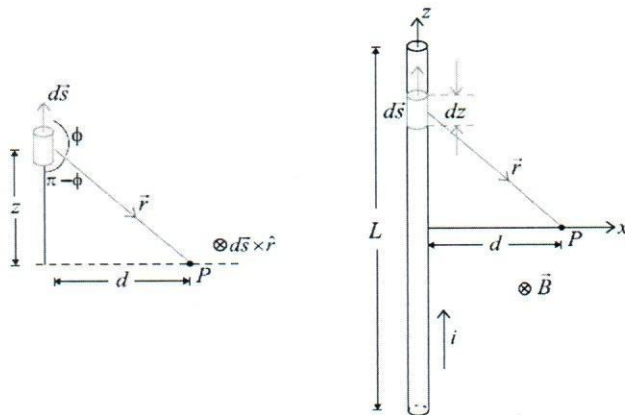


Figure 3

- e) A proton is released from rest in a uniform electric field that has magnitude of 8.0×10^4 V/m and is directed along the positive x-axis. The proton undergoes a displacement of 0.50 m in the direction of electric field. Find the change in electric potential and potential energy respectively of the proton for the displacement. [6]

QUESTION FIVE [20 Marks]

- a) A parallel plate capacitor of capacitance 1 pF has dimensions 5 cm by 10 cm separated by a paper of thickness d millimeters. Find the thickness of this dielectric. ($k=2$). [4]
- b) What is maximum charge that can be placed on this capacitor? (dielectric strength of paper is 16×10^6 V/m) [4]
- c) Find the electric field due to a non-conducting, infinite plane of positive charge with uniform surface charge density σ . [6]
- d) Find an expression for the electric potential at a point p located on the perpendicular central axis of a uniformly charged ring of radius a and total charge Q . [6]

.....END.....