



*(Knowledge for Development)*

**KIBABII UNIVERSITY**  
**UNIVERSITY EXAMINATIONS**  
**2021/2022 ACADEMIC YEAR**  
**THIRD YEAR SECOND SEMESTER**  
**MAIN EXAMINATION**  
**FOR THE DEGREE OF BACHELOR OF SCIENCE**

**COURSE CODE: STA 323**

**COURSE TITLE: QUALITY CONTROL AND ACCEPTANCE SAMPLING**

**DATE: 31/08/2022**

**TIME: 2:00 PM - 4:00 PM**

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**INSTRUCTIONS TO CANDIDATES**

Answer Question One and Any other TWO Questions

TIME: 2 Hours

This Paper Consists of 3 Printed Pages. Please Turn Over.

### QUESTION ONE (30 MARKS)

- a) Briefly describe the important steps in constructing an  $\bar{x}$  - chart [6mks]
- b) Give the three main objectives of a control chart [3mks]
- c) What are the main applications of a control chart [4mks]
- d) Briefly compare the single sampling plan and the double sampling plan [2mks]
- e) Explain briefly how you use control chart for fractional defective ( $p$  - chart) to determine whether the process is in control or not and hence show its warning and action limit on a p-chart. (take  $\alpha = 0.002$  for action limit and  $\alpha = 0.05$  for warning limit) [7mks]
- f) If  $n$  is large and  $p$  is moderately small and we let  $\lambda = np$ , obtain C-chart for the number of defectives per unit. (Take  $\alpha = 0.001$  for action limit and  $\alpha = 0.025$  for warning limit) [8mks]

### QUESTION TWO (20 MARKS)

- a) A company purchases large lots of items using a single sampling plan for which  $n = 4$  and  $c = 0$
- i. Find the probability of acceptance of a lot in terms of proportion of defective items it contains. [2mks]
- ii. What is the probability of
1. A lot containing 50% defective being accepted [2mks]
2. A lot containing 10% defective being rejected [2mks]
- iii. Estimate the AQL ( $\theta$ ) corresponding to a producers risk of 5% and LTPD ( $\theta$ ) corresponding to consumer's risk of 10% [3mks]
- iv. If rectification is agreed on, find the expression for the average outgoing quality (AOQ) in terms of the incoming quality. Find AOQ if  $\theta = 0.05$  [2mks]
- v. Calculate the average total inspection (ATI) of lots of size 100 of quality  $\theta = 0.05$  [3mks]
- b) What do you understand by the moving average chart? Explain clearly how you can use it to determine whether a system is out of control or not. [6mks]

### QUESTION THREE (20 MARKS)

- a) suppose that the mean has shifted from  $\mu$  to  $\mu^*$  but  $\sigma^2$  remain unchanged assuming normality (take  $\alpha = 0.002$ )
- i. Find the probability that the process is under control for the  $\bar{x}$  - chart [4mks]
- ii. Show that the Average Run Length function of the  $\bar{x}$  - chart is given by  $\frac{1}{1-P(\theta)}$ . Assuming that samples taken from the process are independent, where  $\theta$  is the incoming quality [3mks]
- b) Workout the O.C curve and the ARL function for  $S^2$ -chart with upper warning limits given by  $P[\sum (x_i - \bar{x})^2 > k] \leq 0.05$  and action is taken only if two consecutive values of  $S^2$  fall beyond the upper warning limit (take  $n = 12$ ,  $\theta = \frac{\sigma^{2*}}{\sigma}$  and  $\theta \rightarrow (-\infty, 0, \infty)$ ) [6mks]
- c) i. Construction a sequential sampling plan from a Bernoulli population with the following values  $\theta_0 = 0.02$ ,  $\theta_1 = 0.08$ ,  $\alpha = 0.05$  and  $\beta = 0.1$  [4mks]
- ii. An inspector tests 40 units from a large lot. Would he have come to a decision to reject or accept the lot if he found the 10<sup>th</sup>, 18<sup>th</sup> and 23<sup>rd</sup> unit defective? [3mks]

**QUESTION FOUR (20 MARKS)**

- a) Obtain a single sampling for the proportion of defectives, fixing the producer's risk  $\alpha = 0.01$  at  $\theta_1 = 0.05$  and the consumer's risk  $\beta = 0.1$  at  $\theta_2 = 0.1$  and hence give your conclusion **[6mks]**
- b) The data below are samples means and sample ranges for ten consecutive samples, each sample consisting of five measurements of a continuous random variable  $x$ . Assuming  $x$  is normally distributed plot  $\bar{x}$  - control chart and comment on the degree of control

Sample No.	1	2	3	4	5	6	7	8	9	10
Sample mean	136.2	137.4	136.6	139.8	136.0	135.0	136.8	142.0	137.4	136.2
Sample Range	8	6	7	6	8	7	6	19	6	7

$a_n = 0.4299$  for  $n = 5$

**[7mks]**

- c) When do we use  $S^2$ - chart? Explain clearly how you can use it to determine whether a system is out of control or not. If  $n = 4$  and  $\alpha = 0.02$ , obtain its upper action and warning limits. **[7mks]**

**QUESTION FIVE (20 MARKS)**

- a) Explain each of the following concepts
- i. Average sampling numbers [ASN] **[2mks]**
  - ii. Average outgoing quality [AOQ] **[2mks]**
  - iii. Acceptance Quality Level [AQL] **[2mks]**
  - iv. Lot tolerance percent defective (LTPD) **[2mks]**
- b) A large batch of items to be inspected using a single sampling scheme specified by the following values  $n = 40$ ,  $c = 2$ ,  $\theta_1 = 0.02$ , and  $\theta_2 = 0.1$
- i. Define the operating characteristic of this sampling plan **[1mk]**
  - ii. Find the probability of accepting a lot of quality  $\theta = 0.05$  **[2mks]**
  - iii. Find the consumer's risk and the producer's risk **[3mks]**
- c) A large batch of items is to be tested by using double sampling inspection scheme specified by the following numbers  $n_1 = 20$ ,  $n_2 = 40$ ,  $c_1 = 0$ ,  $c_2 = c_3 = 2$
- i. Obtain an expression for the probability of accepting a batch in which the true proportion of defective is  $\theta$  **[3mks]**
  - ii. Obtain the value of this probability when  $\theta = 0.05$  and  $\theta = 0.1$  **[3mks]**