On convergence of sections of sequences in Banach spaces

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Abstract

An elementary proof of the (known) fact that each element of the Banach space $\ell_w^p(X)$ of weakly absolutely*p*-summable sequences (if $1 \le p \le \infty$) in the Banach space *X* is the norm limit of its sections if and only if each element of $\ell_w^p(X)$ is a norm null sequence in *X*, is given. Little modification to this proof leads to a similar result for a family of Orlicz sequence spaces. Some applications to spaces of compact operators on Banach sequence spaces are considered.

Key words and phrases

weak ℓ^{p} -sequences Orlicz sequence spaces compact operators