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(Knowledge for Development)

KIBABII UNIVERSITY
UNIVERSITY EXAMINATIONS
2019/2020 ACADEMIC YEAR
SECOND YEAR FIRST SEMESTER
SPECIAL/SUPPLEMENTARY EXAMINATION
FOR THE DEGREE OF BACHELOR OF SCIENCE

COURSE CODE: MAT 251

COURSE TITLE: **ENGINEERING MATHEMATICS I**

DATE: 05/02/2021

TIME: 8 AM -10 AM

INSTRUCTIONS TO CANDIDATES

Answer Question One and Any other TWO Questions

TIME: 2 Hours

This Paper Consists of 3 Printed Pages. Please Turn Over.

QUESTION ONE (30 MARKS)

Evaluate the integrals

(a) $\int_0^1 e^{2x} \cos 3x dx$ [7 marks]

(b) $\int \frac{3x-2}{(x+2)(x+3)(x-2)} dx$ [8 marks]

(c) Expand $\cos^4 \theta$ by Demoivres theorem [8 marks]

(d) Determine the Eigen values and the corresponding Eigen vectors of the matrix A

$$A = \begin{bmatrix} 1 & 2 \\ 0 & 3 \end{bmatrix}$$
 [7 marks]

QUESTION TWO (20 MARKS)

(a) Expand by Maclaurin's series

(i) $\ln(1+x)$

(ii) $\ln(1-x)$

(iii) $\ln \frac{(1+x)}{(1-x)}$

and hence determine $\ln 4$

[10 marks]

(b) Determine the Taylor's series expansion of $\sin(x+h)$ up to fourth term and hence determine $\sin 44^\circ$

[10 marks]

QUESTION FOUR QUESTIONS (20 MARKS)(a) given that $Z_1 = 3 + 2j$, $Z_2 = 4 - 8j$, $Z_3 = 6 + 9j$ Find (i) $Z_1 + (Z_2 Z_3)$

[4 marks]

(ii) $\frac{Z_3}{Z_1}$

[6 marks]

(b) Expand

(i) $\cos 5\theta$

(ii) $\sin 4\theta$ and hence

(iii) Expand $\tan 5\theta$ by Demoivres theorem

[10 marks]

QUESTION FOUR (20 MARKS)

Determine the Eigen values and the corresponding Eigen vectors of matrix

$$B = \begin{bmatrix} 4 & 3 & 1 \\ 2 & 1 & -2 \\ 1 & 2 & 1 \end{bmatrix}$$

QUESTION FIVE (20 MARKS)

- (a) Differentiate $\cos x$ from the first principles [6 marks]
- (b) $\int x \sin^{-1} x dx$ [6 marks]
- (c) Determine the Maclaurin's series of $\sin^2 x$ up to the third term [8mrks]