



*(Knowledge for Development)*

**KIBABII UNIVERSITY**  
**UNIVERSITY EXAMINATIONS**  
**2020/2021 ACADEMIC YEAR**  
**FIRST YEAR SECOND SEMESTER**  
**MAIN EXAMINATION**

**FOR THE DEGREE OF BACHELOR OF EDUCATION AND  
BACHELOR OF SCIENCE**

**COURSE CODE:** STA 121

**COURSE TITLE:** SAMPLE SURVEYS I

**DATE:** 13/07/21

**TIME:** 2 PM -4 PM

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**INSTRUCTIONS TO CANDIDATES**

Answer Question One and Any other TWO Questions

TIME: 2 Hours

**QUESTION 1:**

(a) state three advantages of sampling over complete enumeration ( 3 marks )

(b) Let the sample arithmetic mean  $\bar{y} = \frac{1}{n} \sum_{i=1}^n y_i$  be an estimator of the population mean  $\bar{Y} = \frac{1}{N} \sum_{i=1}^N Y_i$ .

Verify that  $\bar{y}$  is an unbiased estimator of  $\bar{Y}$  under:

i) Simple random sampling without replacement (SRSWOR), ( 4 marks )

ii) Simple random sampling with replacement (SRSWR). ( 4 marks )

(c) Consider the estimation of  $\bar{y}$  under SRSWOR and SRSWR. Which of these two sampling schemes is more efficient in carrying out the estimation? ( 4 marks )

(d) (i) Describe stratified sampling ( 6 marks )

(ii) Given the following data

Stratum, h	$N_h$	$S_h$
1	45	10
2	20	19
3	65	5

For a fixed sample size,  $n = 60$ , obtain  $n_h$  under the ,

(i) Optimum allocation scheme ( 3 marks )

(ii) Proportional allocation scheme ( 3 marks )

(iii) Neyman allocation scheme ( 3 marks )

**QUESTION 2:**

(a) Distinguish Cluster from Stratified sampling scheme ( 4 marks )

(b) Suppose it is desired that the coefficient of variation, CV of  $\bar{y}$  should not exceed a given or pre-specified value of coefficient of variation, say  $C_0$ , then the required sample size  $n$  is to be determined such that,

$$CV(\bar{y}) \leq C_0 \text{ or } \frac{\sqrt{\text{var}(\bar{y})}}{\bar{Y}} \leq C_0$$

Under these conditions, show that the smallest possible sample size  $n_{smallest}$  is given by

$$n_{smallest} = \frac{C^2}{C_0^2}, \text{ where } C \text{ is the population coefficient of variation ( 16 marks )}$$

**QUESTION 3:**

- (a) Given that  $p$ , a sample proportion is an unbiased estimator of a population proportion  $P$ , use the knowledge of  $Var(\bar{y})$  to derive an expression for the  $Var(p)$ . (7 marks)
- (b) Assuming both  $N$  and  $n$  are large then  $\frac{p - P}{\sqrt{Var(p)}}$  is approximately standard normal,  $N(0,1)$ . Use this idea to write down the confidence interval of  $P$  at  $\alpha$  level of significance. (4 marks)
- (c) Illustrate how you would obtain sample size by fixing the confidence interval length (9 marks)

**QUESTION 4:**

- (a) Describe Cluster Sampling procedure (4 marks)
- (b) Distinguish Cluster from Systematic sampling scheme (3 marks)
- (c) Suppose the number of words in a certain book is to be estimated. It is known that the book has 8 chapters and a total of 450 pages. A random sample of 4 chapters is selected using the simple random sampling procedure and the number of pages in the selected chapters is obtained. The data is given below.

Chapter	No. of pages( $M_i$ )	Total no. of words	$S_i$
1	36	9650	252.96
2	52	12191	265.49
3	98	20845	311.74
4	66	16022	294.65

Obtain

- (i) The mean number of words per page (6 marks)
- (ii) The total number of words in the book (7 marks)

**QUESTION 5:**

- (a) Consider a relatively large sample of size  $n$ . Let the sample be randomly divided into  $k$  groups each of size  $m$  units such that  $n = mk$ .

Let  $\hat{S}^2$  be the estimator of population variance  $S^2$  and be defined as

$$\hat{S}^2 = \frac{m}{k-1} \sum_{i=1}^k (\bar{y}_i - \bar{y})^2$$

Show that  $E(\hat{S}^2) = S^2$ . Comment on the result.

(10 marks)

- (b) The variance,  $s^2$  of a sample of size  $n$  may be given by

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2$$

Verify that the sample variance,  $s^2$  is an unbiased estimator of the population variance,  $S^2$ .

(10 marks)