

# A Review of Algorithms for Determination of Attackability Metrics

<sup>1</sup>Samuel Mungai Mbuguah, <sup>2</sup>Geoffrey Muchiri Muketha, <sup>3</sup>Franklin Wabwoba

<sup>1,3</sup> Kibabii University College, <sup>2</sup> Meru University College

[smbugua@kibabiiuniversity.ac.ke](mailto:smbugua@kibabiiuniversity.ac.ke), [gimuchiri@gmail.com](mailto:gimuchiri@gmail.com), [fwabwoba@gmail.com](mailto:fwabwoba@gmail.com)

## ABSTRACT

Attackability is a concept proposed recently in literature to measure the extent that a software system or service could be the target of a successful attack. A Holistic predictive attackability metrics model has been proposed in our previous study. Metrics derived from this model, their theoretical and empirical validation were proposed and evaluated. The method of measurement of these metrics is largely manual this paper illustrates algorithms that can be adopted with suitable tools to automate the collections of the attackability metrics.

**Keywords:** *Metrics, algorithms, attackability*

The paper is based on PhD work in information technology sponsored by NACOSTI

## 1. INTRODUCTION

The algorithms on this paper are based on metrics derived from the Conceptual Model for a Holistic Predictive Attackability metric for secure service oriented architecture software [1]. Attackability can be expressed as Mean Attackability =  $r/e$  [2] where

$$e = \sum \frac{Ws - W_{attack}}{Ws} \quad \text{and} \quad r = \sum \frac{Ts - T_{attack}}{Ts} \quad 1$$

Validation of metrics can be done both theoretically and empirically. Muketha et al.,[3] expressed that the main goal of theoretical validation was to establish the theoretical soundness of the metrics. Several researchers such Fenton et al.,[4], Weyuker[5] and Briand et al.,[6] have studied the metrics for quite some time.

Weyuker[5] came up with the properties on which to evaluate a metric. First four properties address how sensitive and discriminative the metric is. The fifth property requires that if two classes are combined their metric value should be greater than metric value of each individual class. The sixth property addresses the interaction between two programs/classes. It implies that interaction between program/class A and program/class B is different than interaction between program/class C and program/class B given that interaction between program/class A and program/class C is same. The seventh property requires that a measure be sensitive to statement order within a program/class. The eighth property requires that renaming of variables does not affect the value of a measure. Last property states that the sum of the metric values of a program/class could be less than the metric value of the program/class when considered as a whole. The principles have been critiqued as being ideal for complexity metrics only.

Briand et al.[6] looked at this and expanded on them by including criteria for evaluating size metrics. Since the proposed attackability metrics are size based

then Briand et al.(1998) approach is more applicable in this case. According to Briand et al.(1998), A *system* S will be represented as a pair  $\langle E, R \rangle$ , where E represents the set of elements of S, and R is a binary relation on E ( $R \subseteq E \times E$ ) representing the relationships between S's elements.

Given a system  $S = \langle E, R \rangle$ , a system  $m = \langle E_m, R_m \rangle$  is a *module* of S if and only if  $E_m \subseteq E$ ,  $R_m \subseteq E \times E$ , and  $R_m \subseteq R$ . This will be denoted by  $m \subseteq S$ .

Briand et al.[6] says size is recognized as being an important measurement concept and defines size of a system S as function  $Size(S)$  that is characterized by the following properties Size.1 - Size.3.

### Property Size.1: Non-negativity

The size of a system  $S = \langle E, R \rangle$  is non-negative  
 $Size(S) \geq 0$  (Size.I) 2

### Property Size.2: Null Value

The size of a system  $S = \langle E, R \rangle$  is null if E is empty  
 $E = \emptyset \Rightarrow Size(S) = 0$  (Size.II) 3

### Property Size.3: Module Additivity

The size of a system  $S = \langle E, R \rangle$  is equal to the sum of the sizes of two of its modules  $m_1 = \langle E_{m1}, R_{m1} \rangle$  and  $m_2 = \langle E_{m2}, R_{m2} \rangle$  such that any element of S is an element of either  $m_1$  or  $m_2$  ( $m_1 \subseteq S$  and  $m_2 \subseteq S$  and  $E = E_{m1} \cup E_{m2}$  and  $E_{m1} \cap E_{m2} = \emptyset$ )  
 $\Rightarrow Size(S) = Size(m_1) + Size(m_2)$  (Size.III) 4

The last property Size.3 provides the means to compute the size of a system  $S = \langle E, R \rangle$  from the knowledge of the size of its—disjoint—modules  $m_e = \langle \{e\}, R_e \rangle$  whose set of elements is composed of a different element  $e$  of E.  $Size(S) = \sum_{e \in E} Size(m_e)$  (Size. IV) 5

Therefore, adding elements to a system cannot decrease its size

For each me, it is either  $Re = \emptyset$  or  $Re = \{ \langle e, e \rangle \}$ .

$$(S' = \langle E', R' \rangle \text{ and } S'' = \langle E'', R'' \rangle \text{ and } E' \subseteq E'') \\ \Rightarrow \text{Size}(S') \leq \text{Size}(S'') \text{ (Size.V)}$$

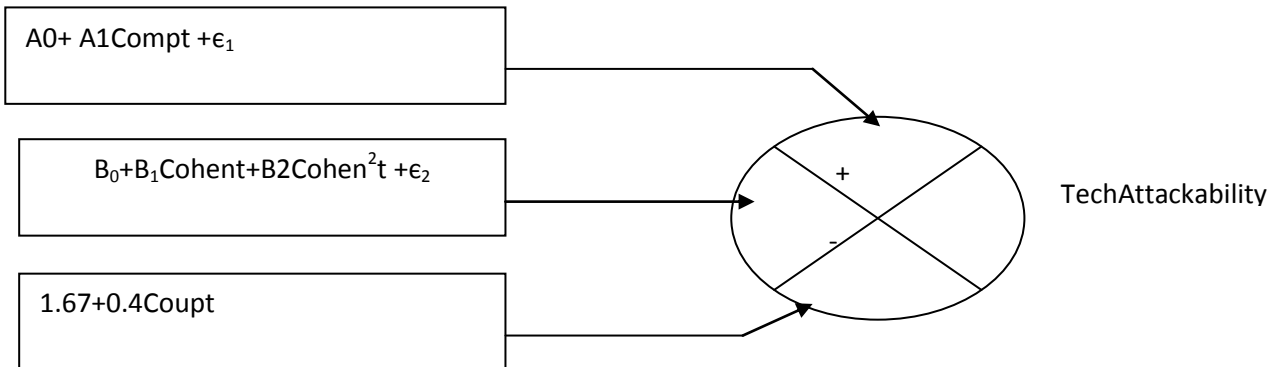
From the above properties Size.1 - Size.3, it also follows that the size of a system  $S = \langle E, R \rangle$  is not greater than the sum of the sizes of any pair of its modules  $m_1 = \langle Em_1, Rm_1 \rangle$  and  $m_2 = \langle Em_2, Rm_2 \rangle$ , such that any element of S is an element of m1, or m2, or both, i.e.,

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = Em_1 \cup Em_2) \\ \Rightarrow \text{Size}(S) \leq \text{Size}(m_1) + \text{Size}(m_2) \\ \text{(Size.VI)}$$

6

The size of a system built by merging such modules cannot be greater than the sum of the sizes of the modules, due to the presence of common elements (lines of code, operators, and class methods). These properties will be used to interrogate the theoretical validity of defined metrics.

The goal of empirically validation of metrics is determine the usefulness of defined set metrics in an industrial setting [3]. It has been argued that there exists



i.  $\text{MeanAttackCompt} = Y + a\text{Compt} + \epsilon_1$

Where MeanAttackComp denotes the attackability due complexity(Comp) an “t” indicates the time element, that the expression is in time domain. Y indicate the point at which if expression was plotted on Y-X axis it could intercept the Y axis. While “a” in the expression represent the gradient of graph which is a limit of the rate of MeanAttackability per unit change in Complexity.  $\epsilon_1$  indicates the random error at time  $t = 0$ .

The assumption for this metric is there is positive correlation between Meanattackability and Complexity(Compt) . It is a statistical model showing causal relationship. It satisfies Size(I) and Size(II) property as defined in section 1. This metric was empirically validated to be true [7]

many metrics yet on few are used in an industrial environment.

## 2. RELATED WORKS

Liu and Troare came up with an algorithm for determination of attackability. This algorithm was used for determining coupling versus attackability. The algorithm was used for implementing equation 1 and not for measuring metrics. In this paper, the algorithms defined are for measuring of the defined attackability metrics.

### 2.1 Technical attackability metrics

Figure 1 is extracted from conceptual holistic predictive attackability model [1] depicting the technical model section. The following were defined as the relationships between mean attackability (mean of attackbility) and the technical attributes (Complexity, Cohesion, Coupling): Figure 1

ii.  $\text{MeanAttackCohent} = X + b\text{Cohent} + \epsilon_2$

Where MeanAttackCohen is meanattackability due to cohesion(cohent), X is Y Axis intercept , b is gradient and  $\epsilon_2$  indicates the random error. The Expression is in the time domain. The assumption for this metric is there is correlation between Meanattackability and Cohesion . It satisfies Size(I) and Size(II) property .

However, from literature it has been stated that the cohesion scale is not linear. If this be the case regression analysis can be used to check for quadratic function.

In that case :  $\text{MeanattackCohent} = X + b_1 \text{cohent} + b_2 \text{cohent}^2 + \epsilon_2$  Where  $b_1$  and  $b_2$  are coefficients of cohen and cohen<sup>2</sup> respectively; The later was verified to be the case [7].

iii.  $MeanattackCoup_t = Z + cCoup_t + \epsilon_3$  9

It is time domain expression indicating a causal relationship between meanattackability due to coupling(coup). Where Z is intercept on Y axis, c is the gradient of the linear graph and  $\epsilon_3$  is the random error.

The assumption for this metric is there is positive correlation between Meanattackability and Coupling. It satisfies Size(I) and Size(II) property. The metrics has been verified to be true[8]. The other two are extension of this metric as applied to complexity and cohesion.

iv.  $TechMeanAttack = (Y-X+Z) + (aComp_t - bCohen_t + cCoup_t) + (\epsilon_1 - \epsilon_2 + \epsilon_3)$  10

Metric (iv) is a new metric defined as a summation of expressions (7,8,&9) of the three attributes working together. It is the Technical MeanAttackability(TechMeanAttack).It satisfies Size (I –III). Coupling and Cohesion work in opposition to each other hence the negative sign in the expression. Through experiments it was found that cohesion

attackability relationship is a quadratic expression, equation 10 changed to

$$TechMeanAttack = (Y-X+Z) + (aComp_t - b_1Cohen_t - b_2Cohen_t^2 + cCoup_t) + (\epsilon_1 - \epsilon_2 + \epsilon_3) [7].$$

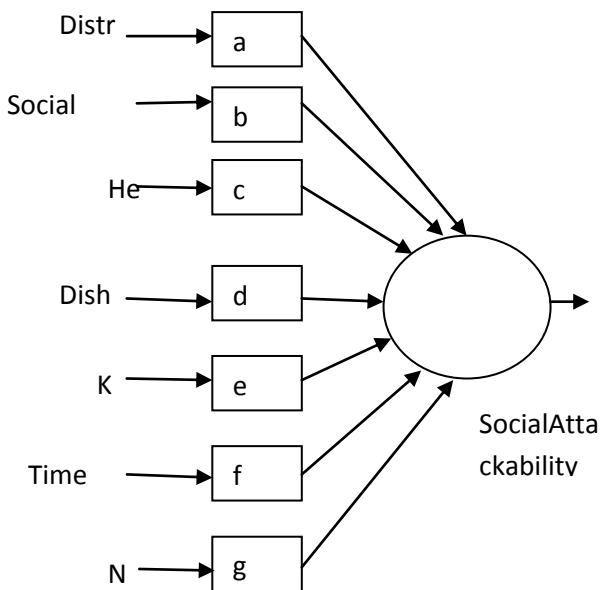
v. Predictive technical attackability metric =  $1/3 \{ (Y-X+Z) + (aComp_t - bCohen_t + cCoup_t) + (\epsilon_1 - \epsilon_2 + \epsilon_3) \}$  11

The purpose of the metric is to try and predict the attackability of software systems knowing the three technical attributes. For this metric the 1/3 is due to probability arising from the sample space of three attributes. For the normalized case and taking discrete values for the attributes then metrics should give us a theoretical maximum of 1 and theoretical minimum of zero. This is within what is expected of probability, a maximum of 1 and minimum of 0.

**2.2 Social Attackability Metrics**

The metric is defined as a summation of each attributes probabilities as indicated in Figure 2 as extracted from conceptual holistic predictive attackability metrics model[1]

Figure 2



Where a,b,c,d,e,f and h represents the probability measures for human traits ( greed, TimePressure(Timep), Kindness(Kind),

Dishonesty(Dish), Herd, Social compliance(socom) and Dist(Distracton).

(i)  $SocAttack = aGreed + bTimep + cKind + dDish + eHerd + fSocom + hDist$  12

Social attackability (SocAttack) represents the system attack due to human traits/attributes that make one susceptible to social engineering attack.

The attributes are measured as percentile scale and taking the floor and ceiling function for attributes i.e. 0 and 1. Then theoretical maximum value is 7 since a, b, c, d, e, f and h have values between 0 and 1 and the attributes taking the discrete case have values varying from 0-1.. The minimum value for metrics will be zero.

(i) Predictive SocAttack metrics=  $1/7(aGreed + bTimep + cKind + dDish + eHerd + fSocom + hDist)$ .

13

Prediction will look at the possibility of even happening and seven attributes have equal probability of occurring hence 1/7. This multiplies equation 12. Since the theoretical maximum of equation 12 is 7 and minimum is 0. The theoretical maximum and minimum of equation 13 are 1 and 0 respectively. This falls within the range of probability and also satisfies Size (I-III). The validation of the equation was done [9]

http://www.cisjournal.org

### 2.3 Holistic attackability metrics

The metrics is defined as composite of technical and social.

Holistic attackability metric = { TechAttack, SocAttack).  
 $= \{ ((Y-X+Z) + (aComp_t - bCohent + cCopt) + (\epsilon_1 - \epsilon_2 + \epsilon_3)) + (aGreed + bTimep + cKind + dDish + eHerd + fSocom + hDist,)$

14

Predictive Holistic attackability metric =  $\frac{1}{2}(\text{TechAttack}, \text{SocAttack})$ .

15

Since TechAttack and SocAttack has maximum value of 1 and minimum of 0.

Then the predictive holistic attackability metrics is also within range. From a theoretical aspect the metrics are theoretical validity for they are within Briand et al.[6] size metrics evaluation criteria. They are also valid from the probability theory[10] perspective.

## 3. ATTACKABILITY METRICS

### ALGORITHM

An algorithm is a method or a process followed to solve a problem. If the problem is viewed as a function, then an algorithm is an implementation for the function that transforms an input to the corresponding output. A problem can be solved by many different algorithms. A given algorithm solves only one problem [11].

By definition, something can only be called an algorithm if it has all of the following properties [11].

- i. It must be correct. In other words, it must compute the desired function, converting each input to the correct output.
- ii. It is composed of a series of concrete steps. Concrete means that the action described by that step is completely understood and doable by the person or machine that must perform the algorithm. Each step must also be doable in a finite amount of time.
- iii. There can be no ambiguity as to which step will be performed next. Often it is the next step of the algorithm description.
- iv. It must be composed of a finite number of steps.
- v. It must terminate. In other words, it may not go into an infinite loop.

It important to write an algorithm to automate any metrics so defined. The researchers discuss an approach that could be used based on matrix multiplication. Consider the multiplication of row and column matrixes

$A_{11} \quad A_{12} \quad \text{and} \quad \begin{matrix} B_{11} \\ B_{12} \end{matrix}$  The product =  $A_{11} \cdot B_{11} + A_{12} \cdot B_{21}$

The result is scalar value, a numeral[10]. This concept can be adopted in an automated collection of the social and technical metrics. For this we require that

coefficient of attributes be read into row matrix and attributes into column matrix then follow the algorithms described below.

Considering the SocAttack metric

**SocAttack = aGreed + bTimep + cKind + dDish + eHerd + fSocom + hDist.**

The algorithm is:

- (i) Read in a, b, c, d, e, f, & h into row matrix
- (ii) Read in (Greed, Timep, Kind, Dishon, Herd, Sococomp, & Dist) into a column matrix
- (iii) Let  $A[k] = \text{multiplying (i) \& (ii)}$
- (iv)  $\text{SocAttack} = a[k]$
- (v)  $\text{Predictive SocAttack} = (\text{iv}) * 1/7$
- (vi) End

Pseudo code

The coefficients in equation 5.6 that is a, b, c, d, e, f and h can be written into a row matrix and the attributes can be written into a column matrix, where an attribute takes values of 1 or 0.

$A[i] = [a, b, c, d, e, f, h]$

$A[j] = [\text{Greed}, \text{Timep}, \text{Kind}, \text{Dishon}, \text{Herd}, \text{Socomp}, \text{Dist}]^{-1}$

For  $(A[j] = 0 \quad A[j] < 8 \quad A[j++])$

$A[k] = \sum A[i] \cdot A[j]^{-1}$

$A[i++]$

Next  $A[j]$

$\text{SocAttack} = A[k]$

$\text{Predictive SocAttack} = 1/7 \quad A[k]$ .

End

Considering TechAttack Metric

$\text{TechMeanAttack} = (Y-X+Z) + (aCompt - b_1Cohent - b_2Cohen^2 + cCopt) + (\epsilon_1 - \epsilon_2 + \epsilon_3)$ . Considering case Cohen<sup>2</sup> not ignored.

Algorithm is:

- (i) Read  $\epsilon_1, \epsilon_2, \epsilon_3$
- (ii) let  $e = \epsilon_1 - \epsilon_2 + \epsilon_3$
- (iii) read Y, X, Z
- (iv) Let  $W = Y - X + Z$
- (v) Read  $a, b_1$  & c into row matrix
- (vi) Read  $b_2$  & Cohen
- (vii) Let  $k = b_2 * \text{cohen}^2$
- (viii) Read complexity, cohesion & coupling into column matrix
- (ix) Let  $A[r] = (v) * (viii)$
- (x)  $\text{TechAttack} = (vii) + (ii) + (iv) + (ix)$
- (xi)  $\text{Predictive TechAttack} = 1/3(x)$
- (xii) End

Pseudocode

Read a, b<sub>1</sub>, b<sub>2</sub>, c, y, x, z,  $\epsilon_1, \epsilon_2, \epsilon_3$ , complexity, cohesion & coupling

$A[m] = [a - b - c]$

http://www.cisjournal.org

```

A[n] = [complexity cohesion coupling]-1
Where an attribute takes the value = 1 or 0
For (A[n] = 0 A[n] < 4 A[n++])
A[r] = ∑A[m].A[n]-1
    A[m++]
    Next n
TechAttack = (y+x+z)+ A[r] +(ε1+ ε2+ ε3)+
b1*cohen2
Predictive TechAttack = 1/3(TechAttack)
End
Consider Holistic Attackability metric
(i) Holistic Attackability metric = [ TechAttack
SocAttack]
(ii) Predictive Holistic Attackability Metric = ½
( predict TechAttack + Predictive SocAttack)
Algorithm
    A[h] = [ TechAttack SocAttack]
    A[p] =½ (predictive TechAttack +
Predictive SocAttack)
End

```

#### 4. CONCLUSION AND RECOMMENDATIONS

The paper main goal was to outline algorithms that could be used to automate the collection of the attackability metrics, the social and technical. The technical model is based on measurement of cohesion, complexity and coupling. There are existing tools such as JHAWK [12] that measure the three metrics directly. Such a tool can be modified to include the algorithms suggested for the technical metrics and generate the resulting technical metrics.

Social metrics is based on measurement of human traits a software tool can be developed to measure these attributes and then social attributes incorporated to generate the overall Social attackability metrics.

Once this is done the holistic predictive attackability metrics can be automated based on discussed algorithm.

There is need for further research on the technical and economically viability of the resulting tool. Asymptotic analysis of the algorithms should be carried out to determine their efficiency and whether there could be alternative algorithms and approaches.

#### REFERENCES

[1]. Mbuguah S.M, Mwangi W., Song P.C, Muketha G.M (2012) A Conceptual Model for a Holistic Predictive Attack Ability Metric for Secure Service Oriented Architecture Software *International Journal of Information and Communication Technology Research* Volume 2 No. 7.

[2]. Liu Y, & Traore I (2007). Complexity Measures for Secure Service-Oriented Architectures. *Third International Workshop on Predictor Models in Software Engineering (PROMISE'07)*. IEEE-COMPUTER SOCIETY.

[3]. Muketha GM.(2011). Size And Complexity Metrics As Indicators Of Maintainability Of Business Process Execution Language Process Models. PhD Thesis, Universiti Putra Malaysia

[4]. Fenton. N(1994) Software measurement: a necessary scientific basis. *IEEE Trans. Software Engineering* pp 199-206

[5]. Weyuker, E.J. 1988. Evaluating software complexity measures, *IEEE Transactions on Software Engineering* 14: 1357-1365.

[6]. Briand, L.C., Morasca, S. and Basilli, V.R. 1996. Property-based software engineering measurement, *IEEE Transactions on Software Engineering* 22: 68-86.

[7]. Mbuguah S.M, Mwangi W., Song P.C, Muketha G.M (2013) Experimental Validation of the Technical Attack ability Metrics Model *International Journal of Information and Communication Technology Research* Volume 3 No. 6,

[8]. Liu M.Y, & Traore I. R. (2009). "Empirical Relations Between Attackability, and Coupling: A case study on DoS,". in *ACM proc. SIGPLAN Workshop on Programming Languages and Analysis for security* ( pp. 57-64.). Ottawa, Canada: ACM

[9]. Mbuguah S.M, Mwangi W., Song P.C, Muketha G.M (2013) Social Attackability Metrics for Software Systems *International Journal of Information and Communication Technology Research* Volume 3 No. 6,

[10]. Stroud K.A.(1993), *Further Engineering Mathematics* Macmillan Press

[11]. Shaffer C.A.(2011), *A practical Introduction to Data structures and algorithm analysis*, E-Book Edition 3.2 Virginia Tech Blackburg.

[12]. JHawk 5 (2010) *Documentation-Standalone User manual Virtual Machinery Version 1.0 Content Copyright © Virtual Machinery.*