



(Knowledge for Development)

KIBABII UNIVERSITY
UNIVERSITY EXAMINATIONS
2017/2018 ACADEMIC YEAR
FIRST YEAR FIRST SEMESTER
MAIN EXAMINATION
FOR THE DEGREE OF BACHELOR OF EDUCATION AND
BACHELOR OF SCIENCE

COURSE CODE: MAT 101

COURSE TITLE: FOUNDATION MATHEMATICS I

DATE: 17/01/18

TIME: 9 AM -11 AM

INSTRUCTIONS TO CANDIDATES

Answer Question One and Any other TWO Questions

TIME: 2 Hours

This Paper Consists of 3 Printed Pages. Please Turn Over.

QUESTION ONE (30 MARKS)

- (a) Define the following terms giving an example in each case
- (i) A set (2mks)
 - (ii) A totology (2mks)
- (b) Given two propositions A and B. Make a truth table for $A \Rightarrow B$. (3mks)
- (c) Taking \mathbb{R} , the set of real numbers as the universal set, give four examples of infinite sets whose complement sets are also infinite. (4mks)
- (d) Let $z_1 = 3 - i$ and $z_2 = -2 + 5i$, find $\frac{z_1}{z_2}$. (4mks)
- (e) How many five letter code words can be formed from the letters of the word ALGEBRA if the code words must begin with A and end with A? (4mks)
- (f) A function f is given by $f: x \rightarrow \frac{1}{|x|-1}$ whose domain is $\{x : x \neq 1, x \neq -1, x \in \mathbb{R}\}$; Show that f is not a bijection. (4mks)
- (g) Given that $\sin A = \frac{3}{4}$ and $0^\circ < A < 90^\circ$, find without using tables the other four trigonometric ratios for angle A (4mks)
- (h) In how many ways can five basketball players be selected from a team of twelve players to participate in a friendly match. (3mks)

QUESTION TWO (20 MARKS)

- (a) Use addition formula to evaluate $\cos 135^\circ$. (4mks)
- (b) Without using tables or a calculator evaluate $\sin 240^\circ$. (2mks)
- (c) Simplify $\cos 80^\circ \cos 20^\circ + \sin 80^\circ \sin 20^\circ$. (2mks)
- (d) Use double angle identities to evaluate $\cos 60^\circ$. (4mks)
- (e) Express $\sin 6x - \sin 4x$ as a product. (3mks)
- (f) Show that $\sin x + \cos x \cot x = \operatorname{cosec} x$ (5mks)

QUESTION THREE (20 MARKS)

- (a) How many 11-letter code words can be formed from the letters of the word INDEPENDENT? (3mks)
- (b) In how many ways can 4 boys and two girls be seated in a row if
- (i) The girls must not be separated (2mks)
 - (ii) The girls are separated (2mks)
- (c) In how many ways can a boy select 3 toffees, 5 chestnuts and 4 berries from a jar containing 8 toffees, 9 chestnuts and six berries? (3mks)
- (d) A box contains 15 balls; 5 of which are red, 4 are green and 6 are blue. In how many ways can 3 balls be chosen if
- (i) There is no restriction? (2mks)

- (ii) The balls are of the same colour? (3mks)
 (iii) The balls are of different colour? (2mks)
 (iv) Only two balls are of the same colour? (3mks)

QUESTION FOUR (20 MARKS)

- (a) If $z = 1 + i$, find the imaginary and the real parts of $z + \frac{1}{z}$. (4mks)
 (b) Given $z_1 = (3 - i)$; $z_2 = 2i$ and $z_3 = 2 - 2i$, show that $|z_1 - z_3| = |z_1 - z_2|$. (5mks)
 (c) Find the fourth roots of i . (6mks)
 (d) If $a = 3 - i$ and $b = 1 + 2i$, evaluate $\frac{a}{2b}$. (3mks)
 (e) Represent $-5 + 6i$ on an Argand diagram. (2mks)

QUESTION FIVE (20 MARKS)

- (a) Given $X = \{2, 4, 6, 8, 10, 12\}$ and $Y = \{2, 3, 4, 5, 6, 7, 8\}$. Determine $n(X \cup Y)$. (4mks)
 (b) Determine the truth tables for the following propositions
 (i) $\sim(A \Rightarrow B) \vee (\sim A \wedge \sim B)$. (7mks)
 (ii) $(A \wedge B) \Rightarrow [\sim(A \vee B) \Rightarrow A]$. (7mks)
 (c) Use a venn diagram to show that the sets $A - B$ and $A \cap B^c$ are equal. (2mks)